

Challenge: Skills and Applications

For use with pages 102–107

In Exercises 1–4, assume that B is the midpoint of \overline{AC} , C is the midpoint of \overline{BD} , and D is the midpoint of \overline{BE} .

- If $BC = 7$, find DE and AE .
- If $CE = 9$, find AB and AE .
- If the coordinate of A is 0 and the coordinate of B is 4, find the coordinates of C , D , and E .
- If the coordinate of B is 3 and the coordinate of E is -9 , find the coordinates of A , C , and D .

In Exercises 5–8, assume that M is the midpoint of \overline{UV} , X is the midpoint of \overline{UM} , and Y is the midpoint of \overline{XV} .

- If $UV = 16$, find UX and XY .
- If $MY = 5$, find XY and UV .
- If the coordinate of X is 7 and the coordinate of Y is 13, find the coordinates of U , M , and V .
- If the coordinate of U is 2 and the coordinate of M is -10 , find the coordinates of X , Y , and V .

In Exercises 9–11, use the diagram shown. Assume that O is the midpoint of \overline{NP} , O is the midpoint of \overline{MQ} , and $\angle N$ and $\angle P$ are right angles.

- If $MN = 15$ and $OP = 8$, find NO and MO .
- If $OP = 28$ and $PQ = 45$, find MO and MQ .
- If $MO = 65$ and $NP = 66$, find PQ and MQ .
- Write a two-column proof. You may use the Pythagorean theorem as a reason.

Given: $AD = 13$, $CD = x$, $BD = 12$,
 $\overline{BD} \cong \overline{AC}$, $\angle C$ is a right angle.

Prove: $x^2 = 25$

